



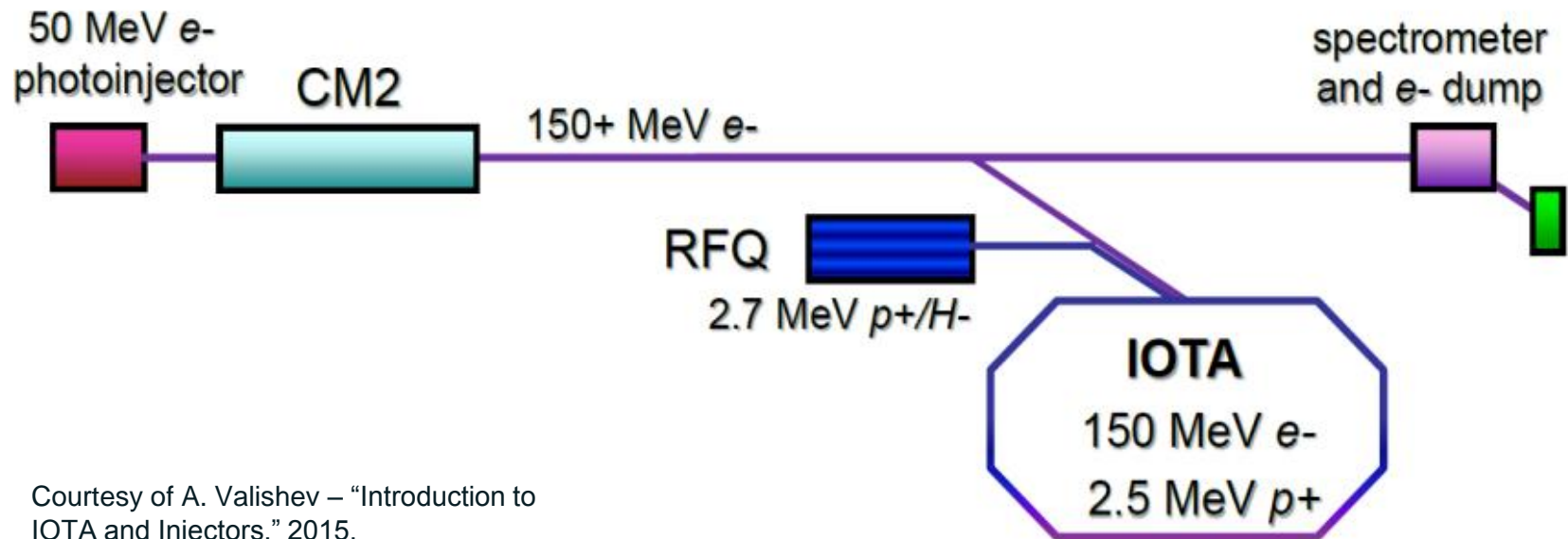
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Implementation of Quadrupole Scan Technique for Transverse Beam Emittance Measurements at Fermilab's Advanced Superconducting Test Accelerator (ASTA)

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Ruan, and Y. M. Shin

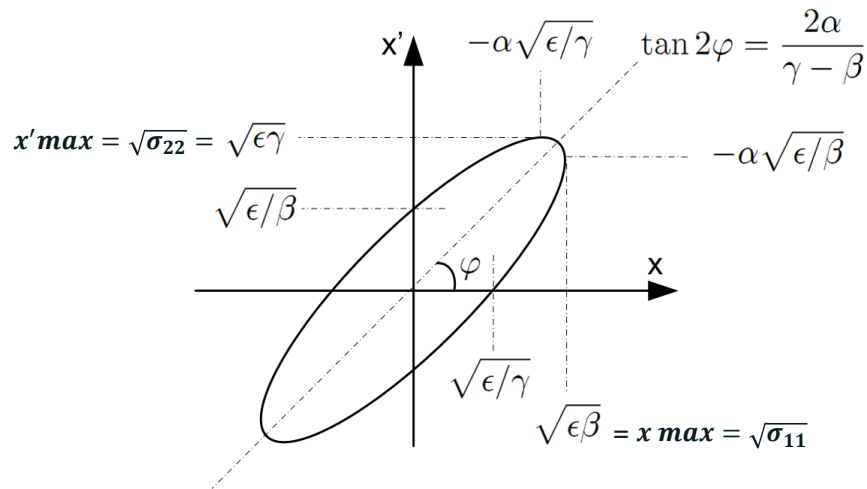
- ASTA
- What is beam emittance?
- Quadrupole magnets and the “thin lens” approximation.
- Quadrupole scan technique.
- Simulated & preliminary experimental results.
- Automation.

Parameter	ILC nominal	Range
Bunch charge	3.2 nC	10pC to > 20 nC
Bunch spacing	333 ns	<10 ns to 10 s
Bunch train	1 ms	1 bunch to 1 ms
Train rep. rate	5 Hz	0.1 Hz to 5 Hz
Transverse emit.	25 mm-mrad	1 to 100 mm-mrad
r.m.s. bunch length	1 ps	10fs to 10ps
Beam energy	300 MeV	50-300 MeV



Courtesy of A. Valishev – “Introduction to IOTA and Injectors.” 2015.

- Emittance is an important characteristic of charged particle beams (describes the quality of a beam).
- 6-D phase space $(x, p_x, y, p_y, z, p_z) \rightarrow$ three 2-D phase spaces \rightarrow three 2-D trace spaces (x, x') , (y, y') , and (z, z') .



Emmanuel Branlard -
<http://emmanuel.branlard.free.fr/work/papers/html/2009fermi/node18>

- The particles of interest can be thought of as being bound by an ellipse and defined by a symmetric moment matrix.

$$\sigma(z) = \begin{vmatrix} \sigma_{11} & \sigma_{12} \\ \sigma_{21} & \sigma_{22} \end{vmatrix}$$

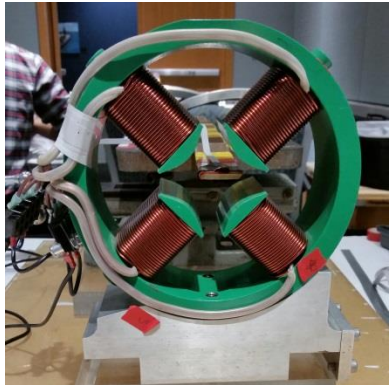
- Liouville's Theorem: area of the ellipse is a conserved quantity.
- Under boosts, only normalized emittance (ϵ_n) is conserved.

- Geometrical emittance:

$$\begin{aligned} \epsilon_x &= \pi \cdot \text{Area} \\ &= \gamma x^2 + 2\alpha x x' + \beta x'^2 \\ &= \pi \cdot \sqrt{\det(\sigma_x)} \end{aligned}$$

- Normalized emittance: $\epsilon_{nx} = \beta\gamma\epsilon_x$

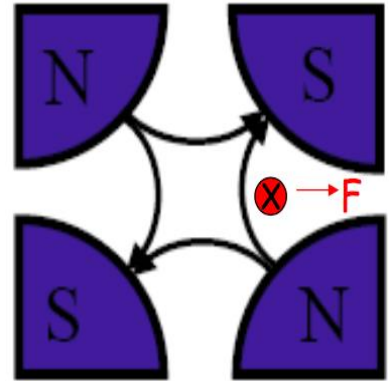
Quadrupole Magnets



- B-field is zero at the center of the quad and increases as you approach the poles.

- From Maxwell's equations:

$$B' = \frac{dB_\phi}{dr} = \frac{8\pi I}{cR^2}$$



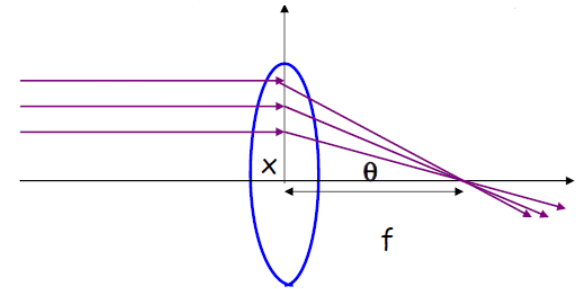
"Magnetic Fields and Magnet Design" – J. Holmes, S. Henderson, Y. Zhang, USPAS. Jan., 2009.

Lorentz Force and RHR:

$$\mathbf{F} = q[\mathbf{E} + (\mathbf{v} \times \mathbf{B})]$$

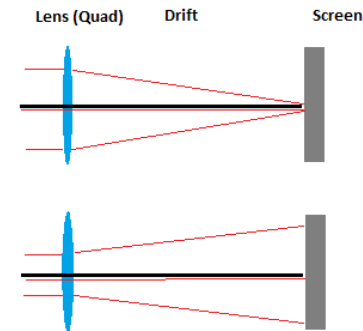
- Positive particle moving into the page would be deflected to the right.

Optical Lens



"Magnetic Fields and Magnet Design" – J. Holmes, S. Henderson, Y. Zhang, USPAS. Jan., 2009.

Magnetic Lens

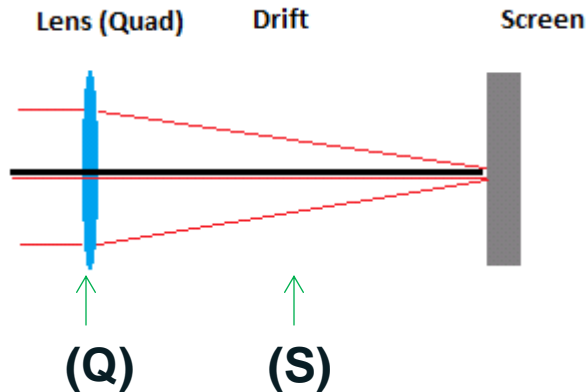


"Magnetic Fields and Magnet Design" – J. Holmes, S. Henderson, Y. Zhang, USPAS. Jan., 2009.

$$\frac{1}{f} = \frac{e}{pc} gL = \frac{gL}{B\rho}, \text{ where } g = \frac{dB_y}{dx}$$

$$k[\text{m}^{-2}] = \frac{1}{fL} = \frac{e}{pc} g = \frac{0.299 g[\text{T/m}]}{\beta E[\text{GeV}]} = \text{focusing strength}$$

“Thin Lens” Approximation



“Thin Lens” Approximation:

- “Thin lens” approximation treats the quad length as zero, while holding the focal length constant.
- $\frac{1}{f} = k \cdot l$, where k is the quad field strength and l is the effective quad length.
- When k is negative \rightarrow focusing quad.
- When k is positive \rightarrow defocusing quad.

$$Q_x = \begin{vmatrix} 1 & 0 \\ kl & 1 \end{vmatrix}$$

“Thick Lens” Model:

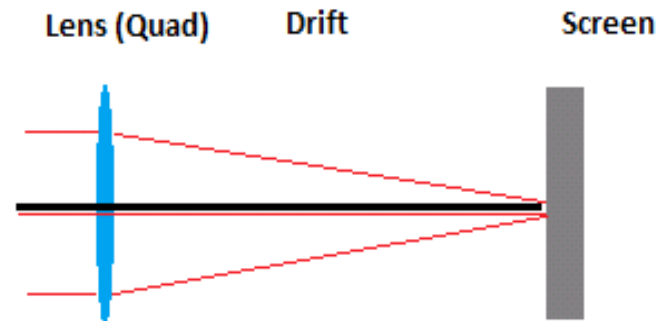
$$Q_x = \begin{vmatrix} \cos\phi & \frac{1}{\sqrt{|k|}}\sin\phi \\ \sqrt{|k|}\sin\phi & \cos\phi \end{vmatrix} \quad [\phi = l\sqrt{|k|}]$$

$$Q_y = \begin{vmatrix} \cosh\phi & \frac{1}{\sqrt{|k|}}\sinh\phi \\ -\sqrt{|k|}\sinh\phi & \cosh\phi \end{vmatrix}$$

$$S = \begin{vmatrix} 1 & L \\ 0 & 1 \end{vmatrix}$$

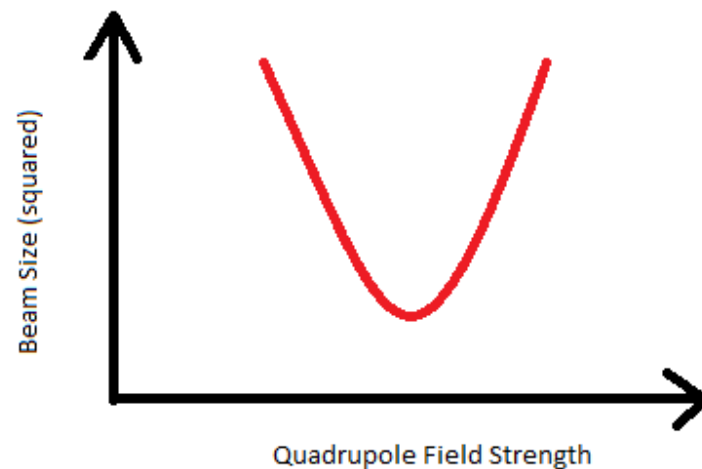
Transfer matrix: $R = SQ \rightarrow \Sigma_f = R\Sigma_i R^T$

1. Select a single quadrupole magnet and an imaging screen (typically a YAG or OTR screen).
2. 'Scan' the magnet by varying the quad field strength and measure the rms beam size on the screen.



Emittance Calculation

- Plot - *beam size*² vs. *quad field strength*.
- Apply a 2nd order polynomial fit to the curve to get three coefficients: $\Sigma_{11} = Ak^2 + Bk + C$
- Using the coefficients, you can calculate the beam matrix elements.
- From the beam matrix (Σ_{beam}), calculate the emittance and C-S parameters.



ASTA

- Quadrupole focusing strength is controlled by power supplies via the ACNET console.
- Focus the beam.
- Find the minimum spot size.
- Scan the quad by varying the current.
- Record the rms beamsizes, via Gaussian fit, on a YAG screen (measured in μm or pixels).

Fig.1: Beam with default quad settings (beam size $< 3\text{ mm}$).

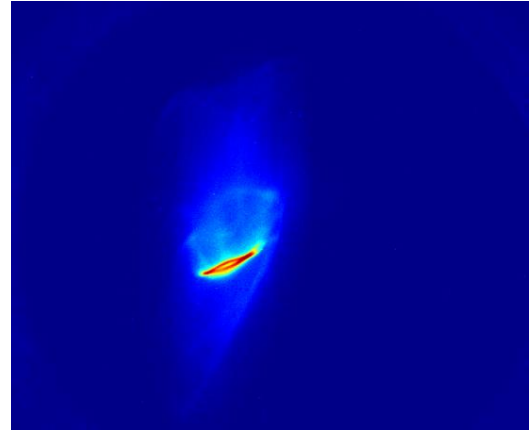
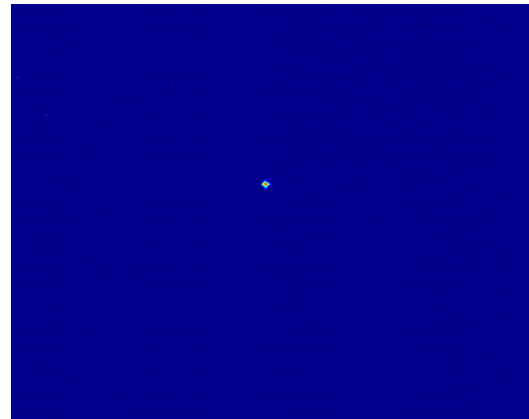
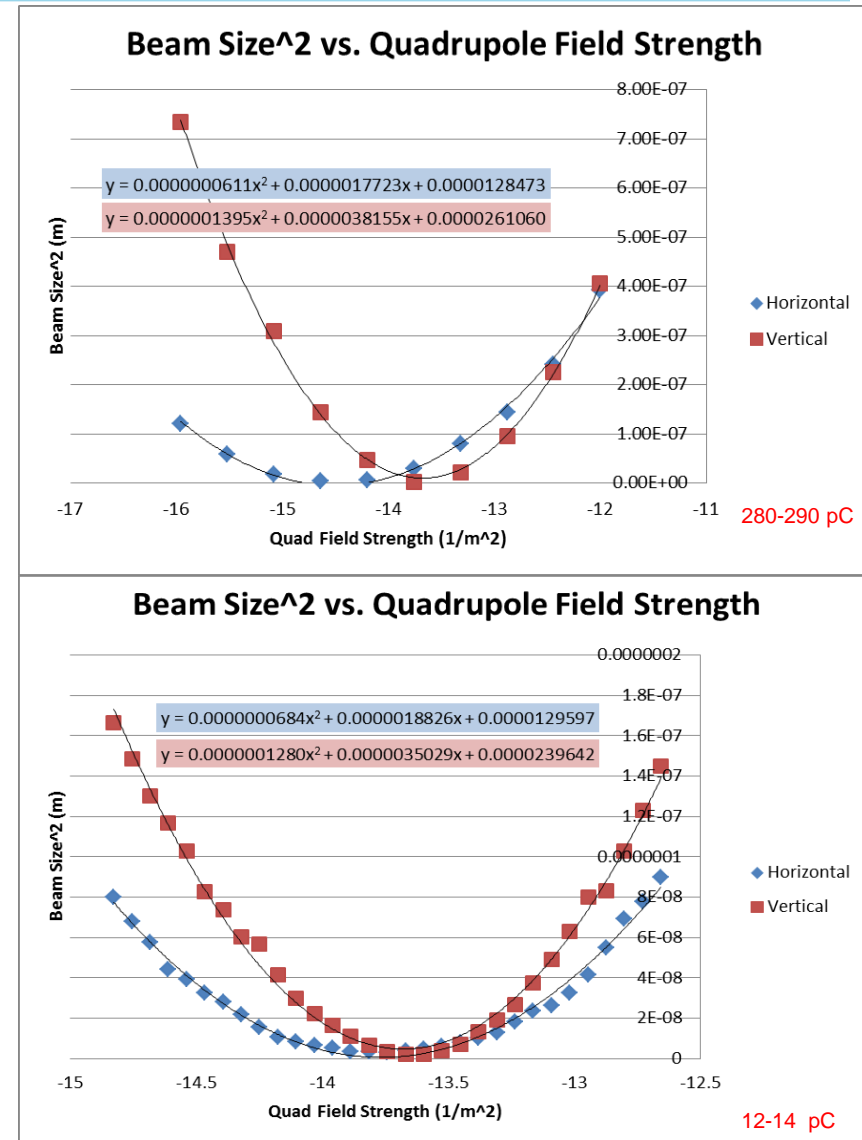


Fig.2: Focused beam (beam size $< 100\text{ }\mu m$).

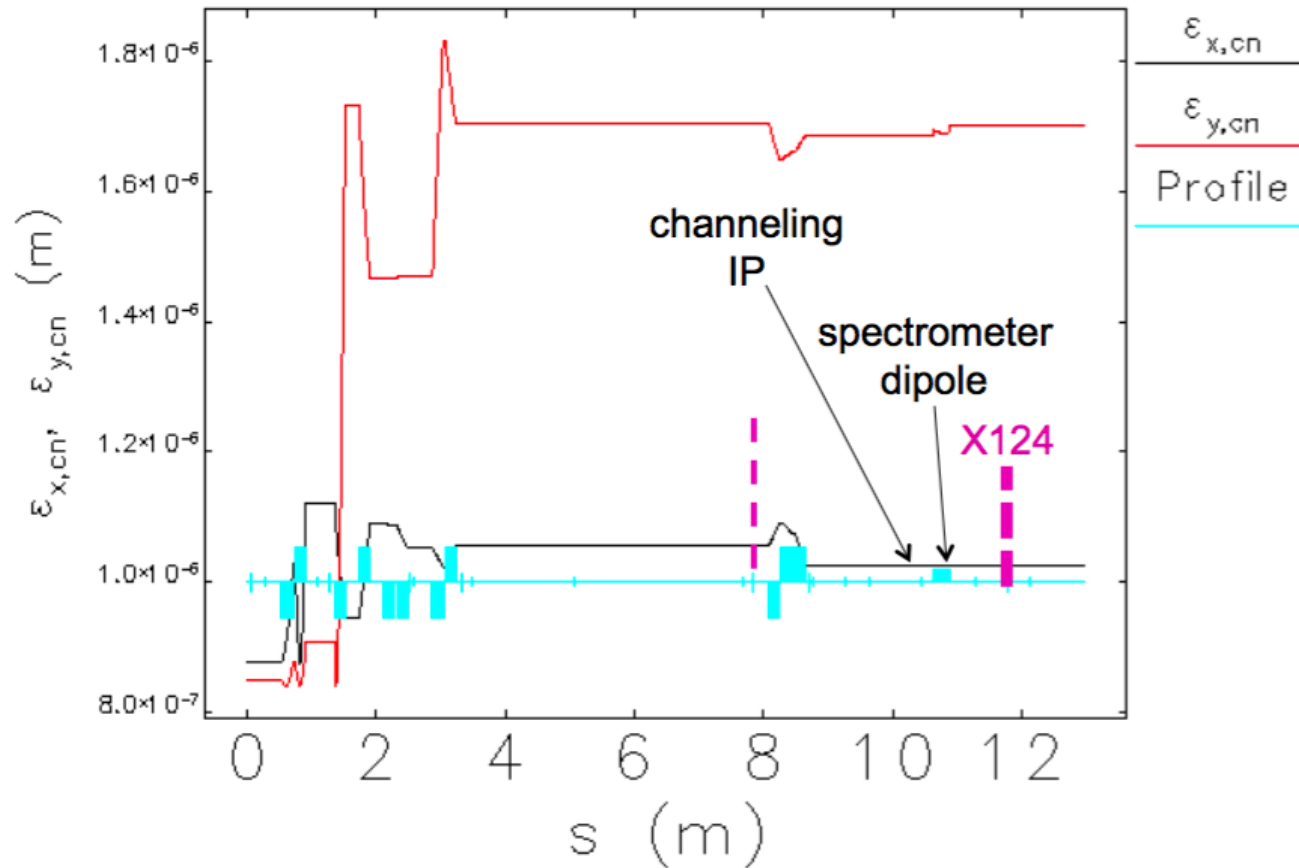


Preliminary Experimental Results

Parameter	Value
Beam Energy	$\sim 20 \text{ MeV}$
Bunch Charge	280 – 290 pC
α_x/α_y	-33.292/25.782
β_x/β_y	21.605/18.349
$\epsilon_{n_x}/\epsilon_{n_y}$	2.95 mm · mrad / 8.14 mm · mrad
Beam Energy	$\sim 20 \text{ MeV}$
Bunch Charge	12 – 14 pC
α_x/α_y	-45.172/45.071
β_x/β_y	31.985/32.185
$\epsilon_{n_x}/\epsilon_{n_y}$	2.05 mm · mrad / 5.06 mm · mrad



Emittance evolution downstream of CAV2



"Possible 1st-beam lattice steup(s) with one cavity" – P.R.G. Piot, IOTA/ASTA User's Meeting, Jan. 2015

Tuning

- Accelerator is still in the commissioning stage and not yet complete.
- Beamline is not fully tuned for optimization.

Thin Lens vs. Thick Lens

- We are currently using the “thin lens” approximation.
- “Thick lens” model will yield more accurate results.

- Preliminary version of automated quad scan used last week:
 - Written in Python.
 - Decreased quad scan time from $\sim 2hr$ to less than $10min$.
- Preliminary version of emittance and C-S parameter calculator written in Python:
 - Enter quad field range and beam parameters.
 - Displays plots, polyfit, geometrical and normalized transverse emittance, C-S parameters.

- ASTA injector/superconducting linac built for high level accelerator R&D.
- Emittance measurements are important for high quality beams.
- Measurements have been taken and are currently being analyzed.
- Shift from “thin lens” approximation to “thick lens” model.
- Further tuning and optimization needed.
- Simple and time saving automated quad scans have been successful.
- Full implementation of automated quad scan/emittance measurements.

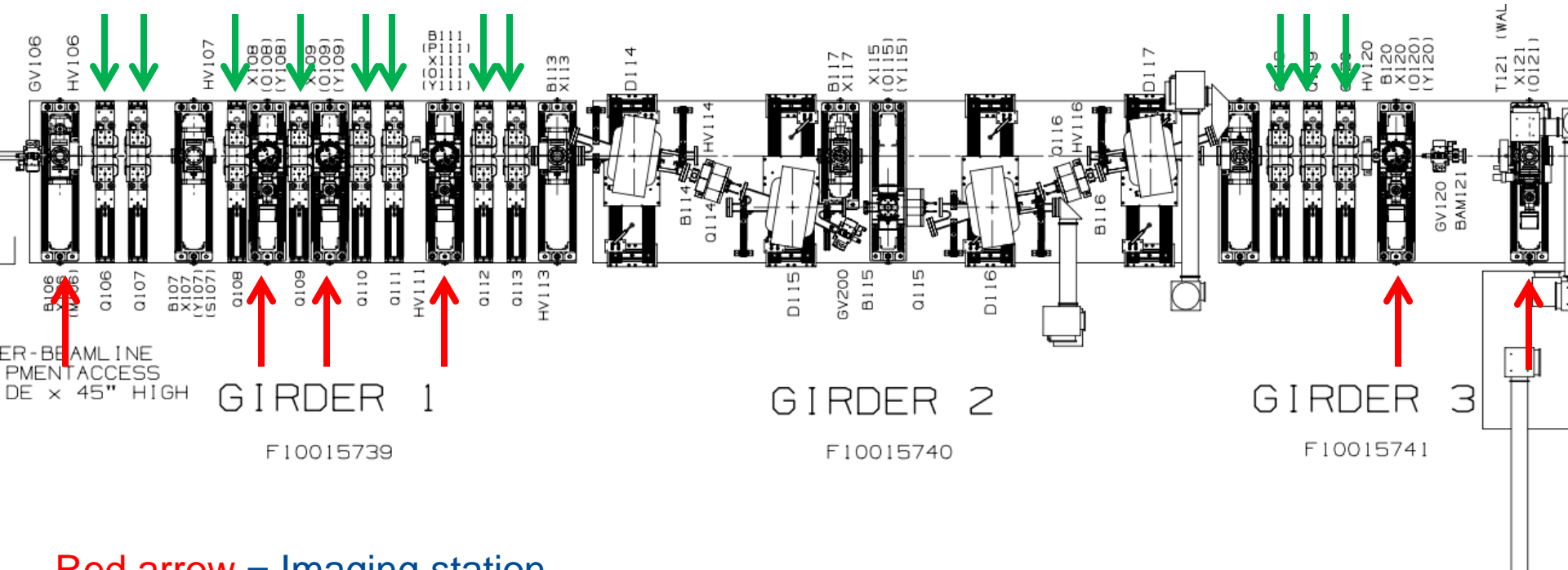
Special thank you to the ASTA operators: Chip Edstrom, Jinhao Ruan, and Darren Crawford

Also, a special thank you to the following for technical discussions and support: Dan Broemmelsiek, Alex Lumpkin, Jamie Santucci, Charles Thangaraj, Giulio Stancari, Sasha Valishev, Philippe Piot, and Young-Min Shin.

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Extra Slides

ASTA Quads/Imaging Screens

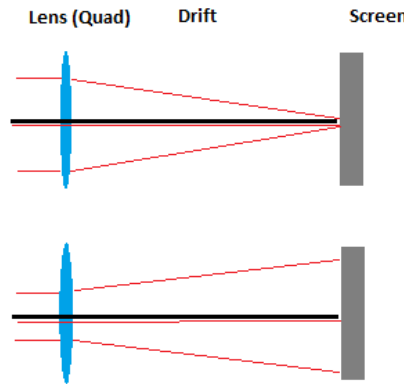


Red arrow = Imaging station

Green arrow = Quadrupole magnet

“Thin Lens” Approximation

- “Thin lens” approximation treats the quad length as zero, while holding the focal length constant.
- $\frac{1}{f} = k \cdot l$, where k is the quad field strength and l is the effective quad length.
- When k is negative \rightarrow focusing quad.
- When k is positive \rightarrow defocusing quad.
- Quadrupole magnets focus in one plane and defocus in the other.



Transfer Matrix

$$R = SQ = \begin{vmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{vmatrix} \cdot \begin{vmatrix} 1 & 0 \\ kl & 1 \end{vmatrix}$$

Solving for emittance

$$\Sigma_{11} = \langle x_f^2 \rangle = (S_{11} + klS_{12})^2 \langle x_i^2 \rangle + S_{12}^2 \langle x_i'^2 \rangle + 2S_{12}(S_{11} + klS_{12}) \langle x_i x_i' \rangle$$

$$\Sigma_{11} = Ak^2 + Bk + C$$

$$\Sigma_{11} = \frac{A}{l^2 \cdot S_{12}^2}$$

$$\alpha = -\frac{\Sigma_{12}}{\epsilon}$$

$$\Sigma_{12} = \Sigma_{21} = \frac{B - 2\Sigma_{11} \cdot l \cdot S_{11} \cdot S_{12}}{2l \cdot S_{12}^2}$$

$$\beta = \frac{\Sigma_{11}}{\epsilon}$$

$$\Sigma_{22} = \frac{C - \Sigma_{11} \cdot S_{11}^2 - 2\Sigma_{12} \cdot S_{11} \cdot S_{12}}{S_{12}^2}$$

$$\gamma = \frac{\Sigma_{22}}{\epsilon}$$